

The Thermodynamics of Refrigeration – Principles of Natural Gas Cryogenic Process

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-----ABSTRACT-----

Refrigeration can be analysed just at a conceptual system level (what purpose it must accomplish, how it can be done in principle, how it can be done in practice), or it can be analysed in more detail to include also the study of the components used in refrigeration equipment: heat exchangers, compressors, valves, absorbers, pumps, piping, supports, controls, selection, design, etc. Here, focus is on refrigeration cycles more than on the actual components used.

Since natural gas liquefies at cryogenic temperatures, i.e. temperatures well below -100°C , there is always a continuous boil-off of the liquefied natural gas during transportation. Accordingly, equipment needs to be provided in order to handle this boil-off.

The basic apparatus is cryogenic tanks (refrigerator), a thermal machine producing cold. The basic principle guarding this process of maintaining that low temperature is known as thermodynamic of refrigeration.

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I. INTRODUCTION

Refrigeration is the withdrawal of heat from a substance or space so that temperature lower than that of the natural surroundings is achieved. It is also the achievement of temperatures below that of the local environment. The main purpose of refrigeration is thermal conditioning (e.g. for food preservation or air conditioning). Refrigeration may be produced by

- Thermoelectric means
- Vapor compression systems
- Expansion of compressed gases
- Throttling or unrestrained expansion of gases.

Producing cold is basically different to and much more difficult than producing heat; people learnt to produce heat 500,000 years ago (in the ice ages), whereas refrigeration started only 150 years ago (in the 19th century).

On mass and economic terms, the transport of liquefied natural gas (LNG) by boat is the largest commercial cryogenic application. From its source, natural gas, compressed to some 6 MPa, is first dried (removing water and liquid hydrocarbons), then sweetened (removing CO_2 and sulphur compounds), lightened (butane and propane removed by cooling to -30°C with a propane refrigeration machine) and then fed to the cryogenic liquefier, after which nitrogen is separated, and the LNG stored aside. The cryogenic liquefier is a vapour-compression-refrigerator (with its condenser cooled by a propane refrigerator at $\square 35^{\circ}\text{C}$) using a working fluid mixture of nitrogen, methane, ethane and propane, that cools the natural gas, at 6 MPa, down to -135°C , before a throttling process to atmospheric pressure yields the final -161°C of storage conditions.

Thermodynamics is the study of the laws that govern the conversion of energy from one form to another, the direction in which heat will flow, and the availability of energy to do work. It is based on the concept that in an isolated system anywhere in the universe there is a measurable quantity of energy called the internal energy (U) of the system.

A thermodynamic system is that part of the universe that is under consideration. A real or imaginary boundary separates the system from the rest of the universe, which is referred to as the *environment*. A useful classification of thermodynamic systems is based on the nature of the boundary and the flows of matter, energy and entropy through it.

There are three kinds of systems depending on the kinds of *exchanges* taking place between a system and its environment:

- *isolated* systems: not exchanging heat, matter or work with their environment. An example of an isolated system would be an insulated container, such as an insulated gas cylinder.

- *closed* systems: exchanging energy (heat and work) but not matter with their environment. A greenhouse is an example of a closed system exchanging heat but not work with its environment. Whether a system exchanges heat, work or both is usually thought of as a property of its boundary, which can be
 - *adiabatic* boundary: not allowing heat exchange;
 - *rigid* boundary: not allowing exchange of work.
- *open* systems: exchanging energy (heat and work) and matter with their environment. A boundary allowing matter exchange is called *permeable*. The ocean would be an example of an open system.

THERMODYNAMICS OF REFRIGERATION

3 Refrigeration

- “refrigeration is the transfer of energy in the form of heat from a colder to a hotter body, by the application of external work” (or heat).
- a refrigerator is most often a reversed ‘heat engine’:



- common methods of refrigeration include:
 1. the vapour compression cycle
 2. the gas compression cycle
 3. absorption cycle
 4. thermoelectric cycle

3.1 Definitions

3.1.1 The coefficient of performance (COP)

- the ‘coefficient of performance’ (*COP*) of a heat pump or refrigerator is analogous to the thermal efficiency (η_{th}) of a heat engine; both quantities define ‘what you get for what you have to put in’
- for a heat engine we ‘get’ work output W , and we have to ‘put in’ heat Q_2 (usually in the form of a combusting fuel) to do so. Thus, from the figure above:

$$\eta_{th} = \frac{\text{work out}}{\text{heat in}} = \frac{W}{Q_2}$$

- the *useful* effect of the refrigerator is the removal of heat from the *cold* space i.e. what we ‘get’ is Q_1 and we have to ‘put in’ work W (usually from a compressor). Thus,

$$COP_{refrig} = \frac{\text{heat removed}}{\text{work required}} = \frac{Q_1}{W}$$

- conversely, the *useful* effect of the heat pump is the addition of heat to a *hot* space i.e. we ‘get’ Q_2 for ‘putting in’ work input W . Thus,

$$COP_{heat\ pump} = \frac{\text{heat supplied}}{\text{work required}} = \frac{Q_2}{W} = \frac{W + Q_1}{W} = 1 + COP_{refrig}$$

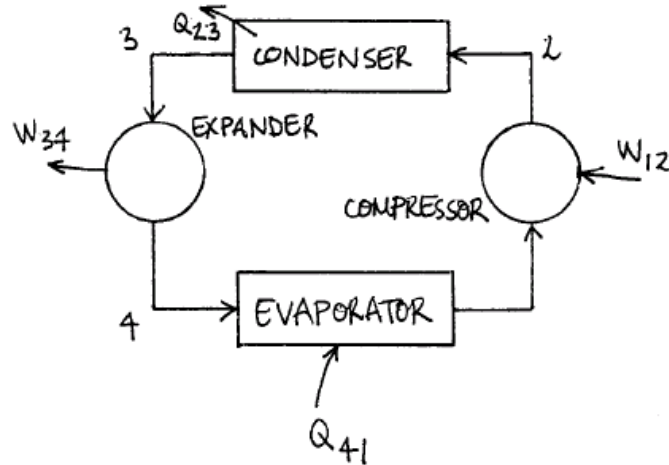
3.1.2 Refrigerating effect and capacity

- the 'refrigerating effect' q (J/kg) is the heat removed per unit mass flow of refrigerant.
- the refrigerating capacity Q (W) is the rate of heat removal.
- the 'ton' is an imperial unit that is still common. It is defined as "1 ton of refrigeration equals the heat transfer required to convert 2000lbm of water at 0°C to ice at 0°C in 24 hours".

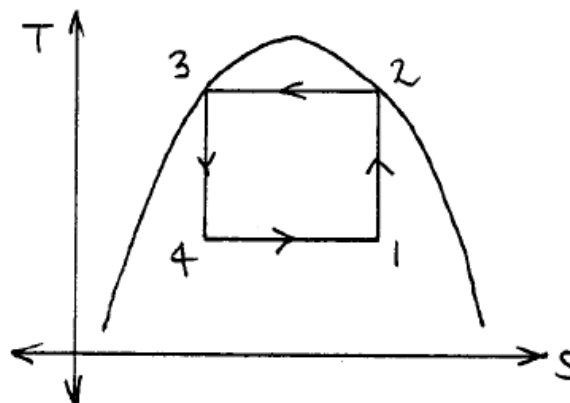
$$1 \text{ ton} = 12000 \text{ Btu/h} = 3.517 \text{ kW}$$

3.2 Simple vapour compression refrigeration cycle

- the simple vapour compressor refrigeration cycle is a reversed Carnot cycle for a condensable working fluid:



- with $T-s$ diagram:

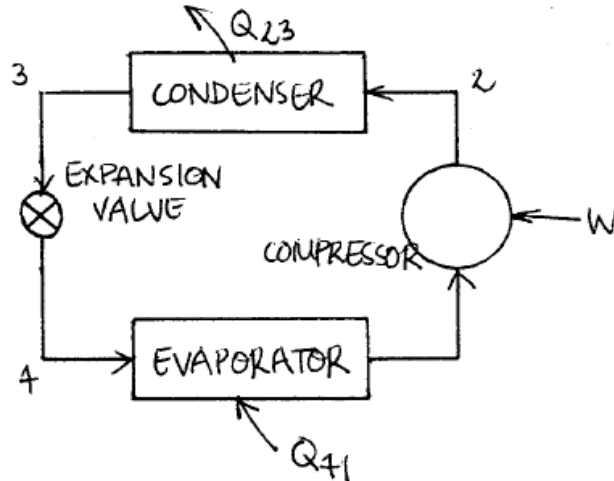


- where:
 - 1 → 2 isentropic (reversible adiabatic) compression
 - 2 → 3 isothermal heat rejection (condensation)
 - 3 → 4 isentropic (reversible adiabatic) expansion
 - 4 → 1 isothermal heat absorption (evaporation)

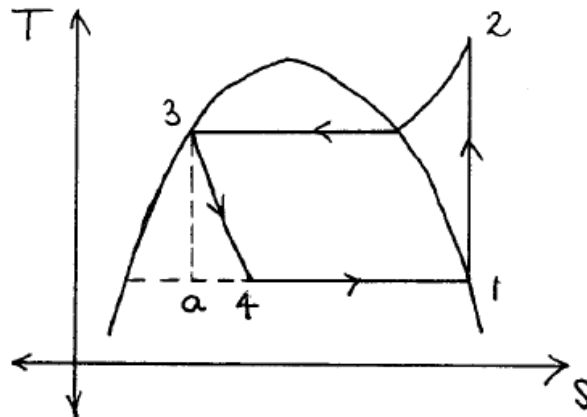
- even allowing for nonisentropic compression and expansion, this cycle is impractical because process 1 → 2 involves the compression of a mixture of liquid and gas until all the liquid has evaporated. This is very difficult to achieve in practice, because the compression of wet mixtures is very difficult to implement mechanically.

3.3 Practical vapour compression refrigeration cycle

- in order avoid the practical difficulties of the simple vapour compression cycle, we make two modifications to it:



- with $T-s$ diagram:



- the two modifications to the simple cycle are:
 1. the expander is replaced by a throttling valve. A throttle is approximately an *isenthalpic* device since, from the SFEE (and neglecting the kinetic energy terms):

$$\underset{=0}{q} - \underset{=0}{w} = \Delta h$$

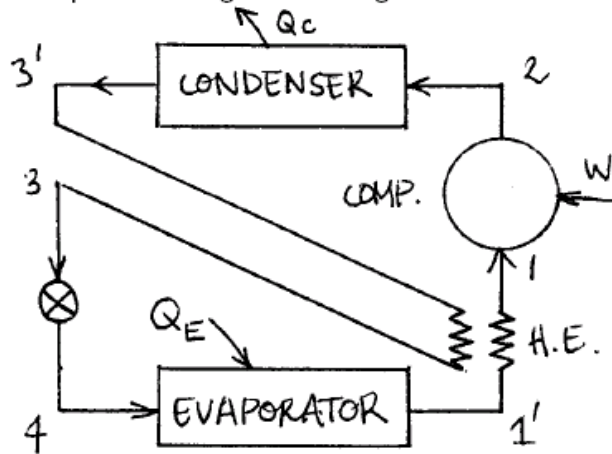
2. the fluid is fully evaporated leaving the evaporator, so the compressor handles *only* a gas
- since throttling creates entropy, the heat transfer in the evaporator is reduced i.e.

$$h_1 - h_4 < h_1 - h_a$$

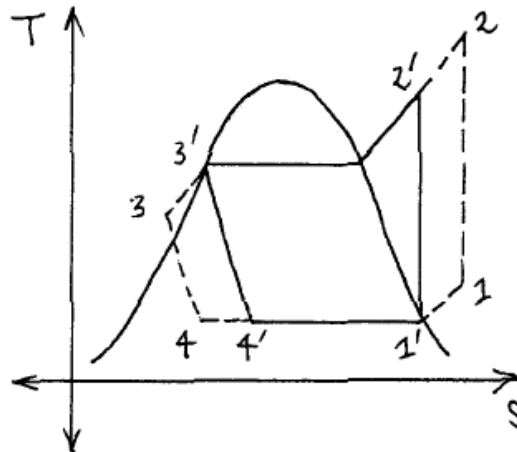
- for a given pressure ratio, the compressor work is larger than for the simple cycle because the compressor delivers a superheated gas
- the cycle COP is less than the COP for the equivalent ideal reversed Carnot cycle since:
 1. condensation is no longer isothermal
 2. throttling is inherently irreversible as is 'real' compression

3.4 Undercooling & superheating

- this is a similar concept to the regenerative gas turbine:



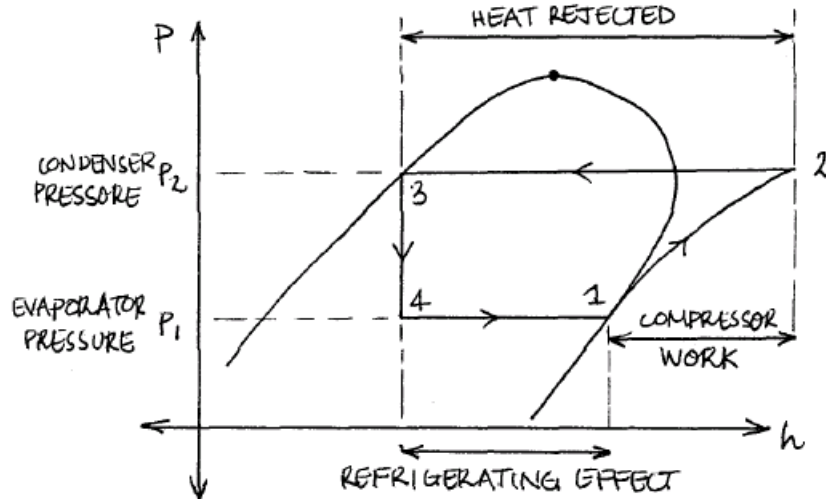
- with $T-s$ diagram:



- note:
 1. condensate from the condenser is cooled, increasing the heat absorbed in the evaporator. Thus, the cooling effect is increased.
 2. vapour is superheated before compression, thus ensuring that no liquid exists in the compressor.
 3. compressor work is increased

3.5 P-h diagram

- the $P-h$ diagram is often used when studying refrigeration cycles because the condenser q_{23} and evaporator q_{41} heat transfer and the compressor work w_c are easily read off the charts.
- the $P-h$ diagram for the practical vapour compression cycle is:



- as is shown, the practical vapour compression refrigeration cycle is comprised of two (ideally) isobaric heat transfer processes (condensation & evaporation) and one isenthalpic process (throttling)
- from the SFEE, and neglecting the kinetic energy terms (note that we have broken the sign convention and made all terms positive in order to simplify the maths):

quantity	q	w
compressor work	0	$w_c = h_2 - h_1$
condenser heat transfer	$q_{23} = h_2 - h_3$	0
evaporator heat transfer	$q_{41} = h_1 - h_4$	0
throttling ($h_3 = h_4$)	0	0

- also, the $P-h$ diagram shows that:

$$q_{41} + w_c = q_{23}$$

- it follows that the COP of various devices can be determined:

$$COP_{refrig} = \frac{q_{41}}{w_c} = \frac{q_{41}}{q_{23} - q_{41}}$$

$$COP_{heat\ pump} = \frac{q_{23}}{w_c} = \frac{q_{23}}{q_{23} - q_{41}} = \frac{q_{41} + q_{23} - q_{41}}{q_{23} - q_{41}} = COP_{refrig} + 1$$

3.6 Refrigerants

- the working fluid within the refrigeration cycle is referred to as a 'refrigerant'. Refrigerants should have the following properties:

property	desired	explanation
Critical temperature	> condenser temperature	To approach the Carnot cycle and hence achieve high <i>COP</i>
Freezing temperature	Low	Liquid only in evaporator. No freezing
Saturation pressure	Above atmospheric	Avoid air leaks into the system.
Evaporation enthalpy	High	Reduces mass flow rate.
Specific volume	Low	Reduces compressor work and system size.
Stability	Good	Both pure substances and mixtures
Thermal conductivity	High	good heat transfer rates
Solubility	Low	Avoid water contamination. Avoid oil contamination
Toxicity/ Irritancy	Low	Avoid poisoning. Convenient handling.
Non-Flammable		Safety in charging, handling. Safety if leaks.
Detectability	Good	For tracing leaks.
Ozone depletion	None	Prevent ozone layer depletion.
Cost	low	

- examples of common *inorganic* refrigerants:
 - ammonia (NH_3)
 - carbon dioxide (CO_2)
 - sulphur dioxide (SO_2)
- examples of common *organic* refrigerants:
 - Trichlorofluoromethane (CFCl_3) – 'Freon 11' or 'R11'
 - Dichlorodifluoromethane (CF_2Cl_2) – 'Freon 12' or 'R12'
 - monofluorodichloromethane (CHFC_2) – 'Freon 21' or 'R21'
 - methylchloride (CH_3Cl)
 - trifluoroethane ($\text{C}_2\text{F}_3\text{Cl}_3$) – 'Freon 113' or 'R113'
 - Tetrafluoroethane (CH_2FCF_3) – 'Freon 134a' or 'R134a'
- in order to protect the ozone layer, new domestic refrigerators and airconditioning units use hydrofluorocarbons (HFC's) as a replacement refrigerant chlorofluorocarbons (CFC's). eg. R134a is a replacement for R12

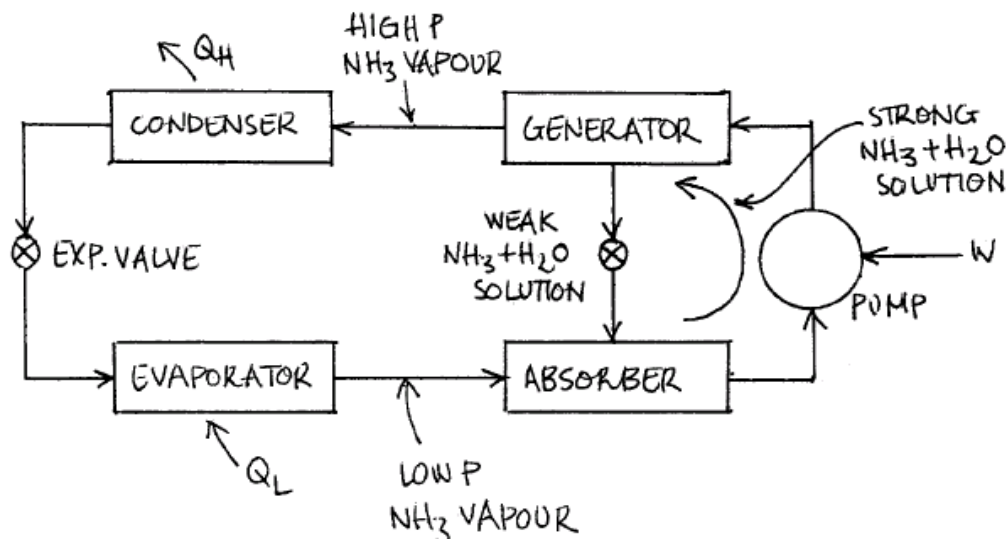
- looking at the properties of ammonia and R12:

Property	Ammonia		Freon 12	
Critical temp	yes	132°C	yes	112°C
Freezing temp	yes	-78°C	yes	-158°C
Saturation pressure	yes	>1 atm, boils at -33°C @ 1 atm	yes	>1 atm
Evaporation enthalpy	Yes	Very high	no	Only 1/8 NH ₃
Specific volume	Yes		yes	
Stability	No	Attacks Cu and alloys of Cu	yes	Non-corrosive
Thermal conductivity	Yes	High		Only 1/10 NH ₃
Solubility	No Yes	Soluble in water Insoluble in oil	yes no	Insoluble Miscible
Toxicity/Irritancy	No No	Toxic Irritates eyes	yes yes	Non-toxic OK
Non-flammable	No	Ignitable	yes	
Detectability		Smells	yes	no smell, special detector needed
Ozone depletion	Yes	No ozone effect		Very bad
Cost	Yes	Very cheap		Expensive

- the more environmentally friendly R134a has very similar properties to R12, but does not cause ozone depletion.

3.7 Ammonia (NH₃) absorption refrigerator

- large scale refrigeration plants often feature this cycle because ammonia has a high specific enthalpy of evaporation (therefore reducing plant size) and the pump specific work is relatively small.



- the objective of this cycle is to replace the vapour compressor with a liquid pump, since the pumping of liquid typically requires much less energy. This is clear since:

$$w = -\int v dP$$

$$\approx -v(P_2 - P_1) \text{ for a liquid}$$

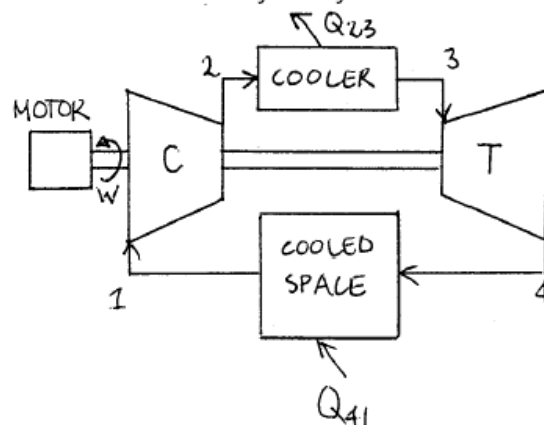
- thus, for a given pressure ratio, the work required to pump a liquid is much smaller than that required to compress a gas since the specific volume v of the liquid is much smaller (density ρ is greater).
- the process can be divided up as follows:
 - the condensation, expansion and evaporation processes consist of NH_3 vapour only, and are in principle the same as these processes in the vapour compression cycle
 - the NH_3 is absorbed into a solution with H_2O in the absorber
 - the liquid solution of $\text{NH}_3 + \text{H}_2\text{O}$ has its pressure raised by the pump
 - the generator is heated to release NH_3 , but H_2O stays in liquid phase because it has a higher boiling temperature
 - the NH_3 proceeds around the cycle and the H_2O is throttled back to low pressure and returns to the absorber

drawbacks:

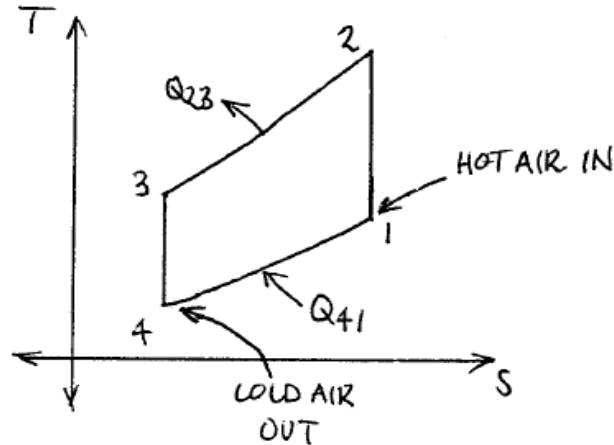
- it can be difficult to keep H_2O out of the NH_3 loop, where the H_2O may freeze in the evaporator.
- cycle requires more components than vapour compression cycle

3.8 Air cycle refrigeration

- air cycle refrigeration is the Joule/Brayton cycle in reverse:



- and with an ideal compressor and turbine, the $T-s$ diagram is:



- note:
 1. unlike the previous cycles, phase changes do not occur within this cycle and it features only a gas
 2. we must have an expansion turbine, not a throttle
 3. in order to achieve reasonable COP , we must have high η_c and η_t

- coefficient of performance:

$$COP = \frac{Q_m}{W_m} = \frac{Q_{41}}{W_c - W_t}$$

- it follows that:

$$COP = \frac{\gamma_p (T_1 - T_4)}{\gamma_p (T_2 - T_1) - \gamma_p (T_3 - T_4)}$$

$$= \frac{\left(1 - \frac{T_4}{T_1}\right)}{\left(\frac{T_2}{T_1} - 1\right) - \frac{T_4}{T_1} \left(\frac{T_3}{T_4} - 1\right)}$$

- note, as discussed earlier, the static temperature is approximately equal to the stagnation temperature if the kinetic energy of the flow is small.

- since processes 1→2 and 3→4 are isentropic, let:

$$\frac{T_2}{T_1} = r_p^{\gamma} = \frac{T_3}{T_4}$$

- where $r_p = p_2 / p_1 = p_3 / p_4$

- thus:

$$COP = \frac{\left(1 - \frac{T_4}{T_1}\right)}{\left(r_p^{\gamma} - 1\right) - \frac{T_4}{T_1} \left(r_p^{\gamma} - 1\right)}$$

- and finally:

$$COP = \frac{1}{\left(\frac{r_p^\gamma}{r_p^\gamma - 1} \right)}$$

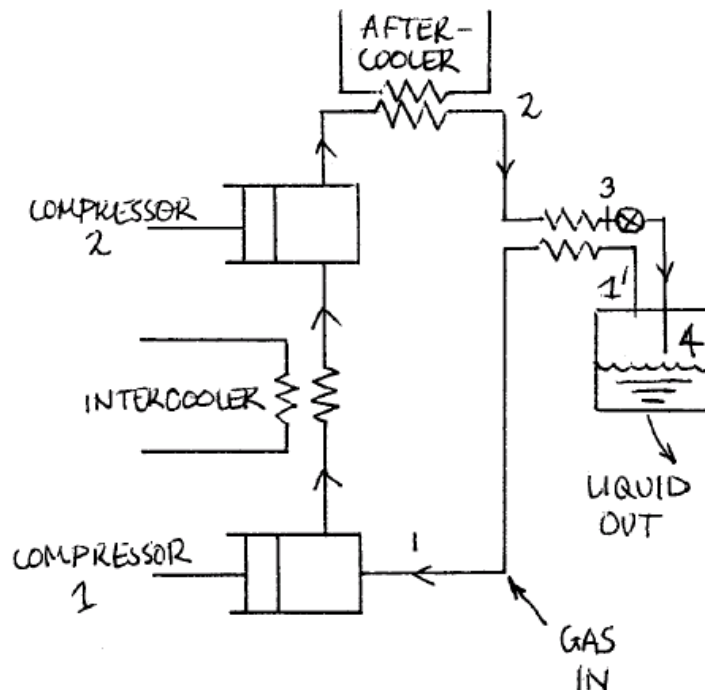
- which shows that the *COP* reduces with increased pressure ratio of. the increase in η_{th} with pressure ratio for the ideal gas turbine cycle shown earlier.

3.9 Liquefaction of gases

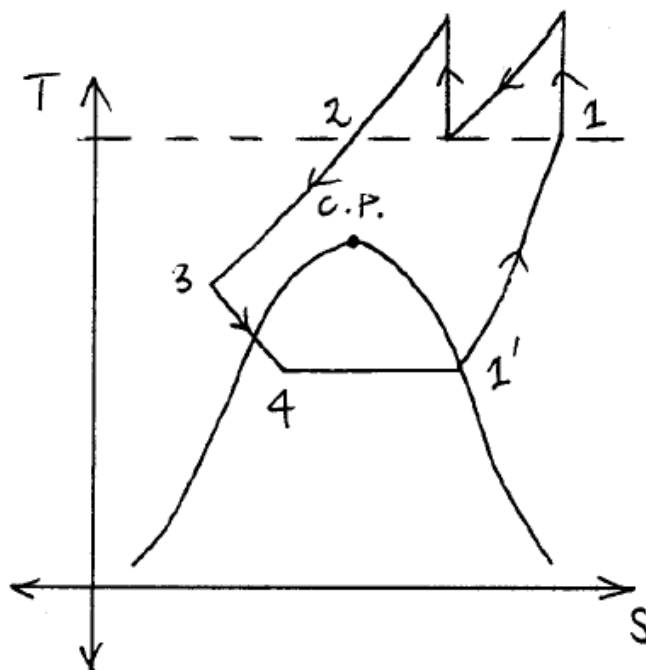
- liquefaction uses the gas to be liquefied as the working fluid
- the liquefaction process must bring the gas state to below its critical point in order for condensation to occur
- critical points of common substances:

Substance	T _{CRIT} (K)	P _{CRIT} (MPa)
CO ₂	304	7.39
O ₂	155	5.08
N ₂	126	3.39
H ₂	33.3	1.30
Ar	151	4.86

- a sketch of a typical liquefaction process:



- and its corresponding $T-s$ diagram:



IV. CONCLUSION

The information provided in this paper and the level of detail for the thermodynamic of refrigeration are intended to demonstrate the competitive edge of this concept with respect to:

- Safety (minimum hydrocarbon inventory in process)
- Reliability
- Operability
- Energy efficiency (minimal CO₂-emission, high condensate yield)
- Economics
- Flexibility

Despite the fact that not all issues were addressed in full detail, it is clear that the refrigeration process can be made very efficient and installed at a sufficiently low cost to be truly competitive.

The development of this concept requires further evaluation with respect to the following issues:

- Integration of the LNG plant with the ship's systems
- Off-loading (this is a separate technology development)
- (Comparative) Safety studies
- More detailed cost estimate of the LNG vessel, off-loading and mooring systems
- Availability & reliability Study

This truly innovative refrigeration technology has lead to a breakthrough in LNG production.

The process of Thermodynamics of refrigeration devices is overwhelming, and refrigeration devices are used in operating applications such as:

1. Upstream: Associated Gas Liquefaction
2. Gas Liquefaction during extended well testing
3. Hydrocarbon dew pointing in gas treatment facilities
4. Remote, marginal field developments
5. Air Separation on drilling rigs (N₂ for well injection)
6. Air Separation in Gas to Liquids plants
7. LNG: Storage and Carrier boil-off re-liquefaction
8. Petrochemical: C₂, C₃-splitting, etc.
9. Energy: Peak Shaving and load management for transmission systems
10. LNG as feedstock for remote, small IPP's

11. Other: LNG vehicle fuelling for fleet operations
12. Coal bed Methane Liquefaction
13. VOC Recovery on tank farms
14. CO₂-recovery, e.g. horticultural

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